# Kernel Mean Matching for <u>Content</u> <u>AD</u>dressability of <u>GAN</u>s

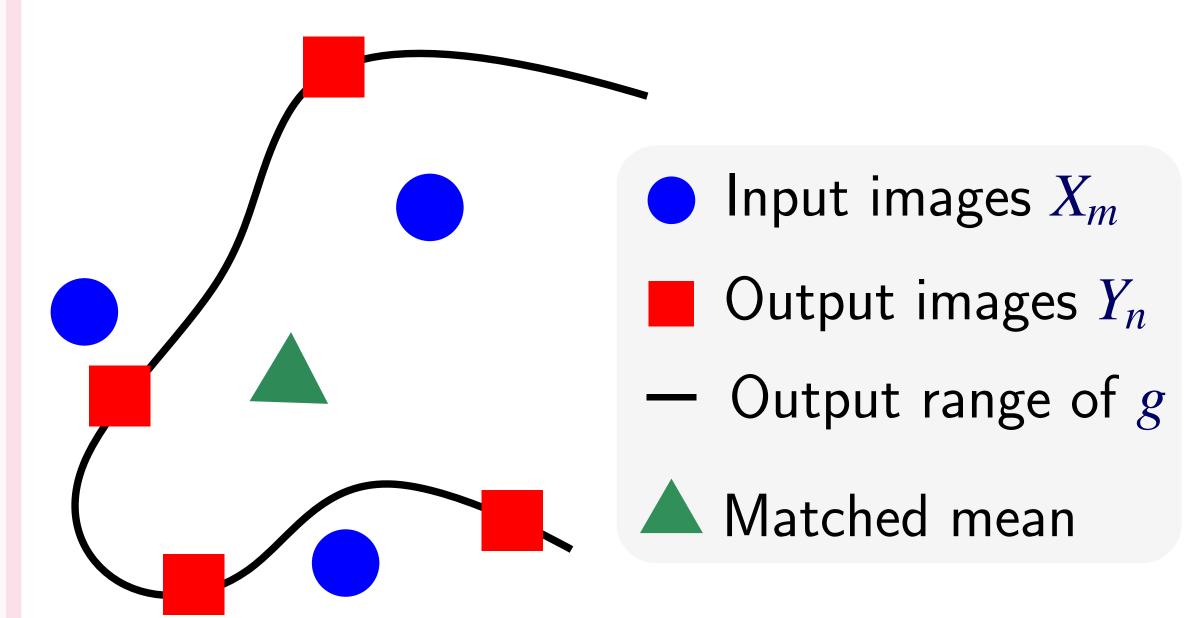
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#### Summary

- **Given**: Pre-trained GAN g, input images  $X_m := \{\mathbf{x}_i\}_{i=1}^m$
- **Goal**: Generate images  $Y_n := \{\mathbf{y}_j\}_{j=1}^n$  similar to  $X_m$ .
- Propose CADGAN: a kernel mean matching procedure that adds "content-addressability" to g at run-time.
- Advantages:
- 1.  $\bigcirc$  No need to retrain g.
- 2. Flexible choice of the similarity criterion.
- 3. Fine-grained control with input weights  $\{w_i\}_{i=1}^m$ .

#### **Proposal: CADGAN**

**CADGAN**: Generate **images** from g so as to match the mean feature of the input images represented in a reproducing kernel Hilbert space (RKHS).



**How**: Minimize the distance (MMD) between the input and output means in RKHS  $\mathcal{H}$  (kernel mean matching):

$$\underset{\{\mathbf{y}_j\}_{j=1}^n \text{ in range}(g)}{\arg\min} \left\| \sum_{i=1}^m w_i \phi(\mathbf{x}_i) - \frac{1}{n} \sum_{j=1}^n \phi(\mathbf{y}_j) \right\|_{\mathcal{H}}^2.$$
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•  $\{\mathbf{y}_j\}_{j=1}^n$  are constrained to be in the output range of g. •  $\phi$ : an implicit nonlinear function (induced by a kernel). •  $w_i$ : weight of the input  $\mathbf{x}_i$ .  $\sum_{i=1}^m w_i = 1$  and  $w_i \in [0, 1]$ .

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## Kernel Mean Matching with a Generator • Let $K(\mathbf{a}, \mathbf{b}) = \langle \phi(\mathbf{a}), \phi(\mathbf{b}) \rangle_{\mathcal{H}}$ be a kernel ( $\approx$ similarity) between two images a, b. • Parametrize $\mathbf{y}_j = g(\mathbf{z}_j)$ where $\mathbf{z}_j$ is a latent vector. Then, (1) can be rewritten as $\sum_{i=1}^{m} w_{i}w_{j}K(\mathbf{x}_{i},\mathbf{x}_{j}) + \frac{1}{n^{2}}\sum_{i=1}^{n} K(g(\mathbf{z}_{i}),g(\mathbf{z}_{j})) - \frac{2}{n}\sum_{i=1}^{m} w_{i}\sum_{i=1}^{n} K(\mathbf{x}_{i},g(\mathbf{z}_{j})).$ (2) i, j=1Proposed CADGAN: $\arg \min_{\{\mathbf{z}_i\}_{i=1}^n} (2)$ • Optimize the latent vectors $\{\mathbf{z}_j\}_{j=1}^n$ with Adam. • Output images: $\{g(\mathbf{z})_j\}_{i=1}^n$ . • Use kernel $K(\mathbf{a}, \mathbf{b}) := k(E(\mathbf{a}), E(\mathbf{b}))$ where E is an image feature extractor of choice e.g., VGG Face, Places365-ResNet. • Use IMQ kernel $k(\mathbf{s}, \mathbf{t}) = (c^2 + ||\mathbf{s} - \mathbf{t}||_2^2)^{-1/2}$ for some c > 0. **Experiment: LSUN-{Bridge, Bedroom, Tower}** Output Output Input Input • 3 GANs from Mescheder et al., 2018 trained on LSUN-bridge, LSUN-bedroom, LSUN-tower. • Extractor E = Places365-ResNet.

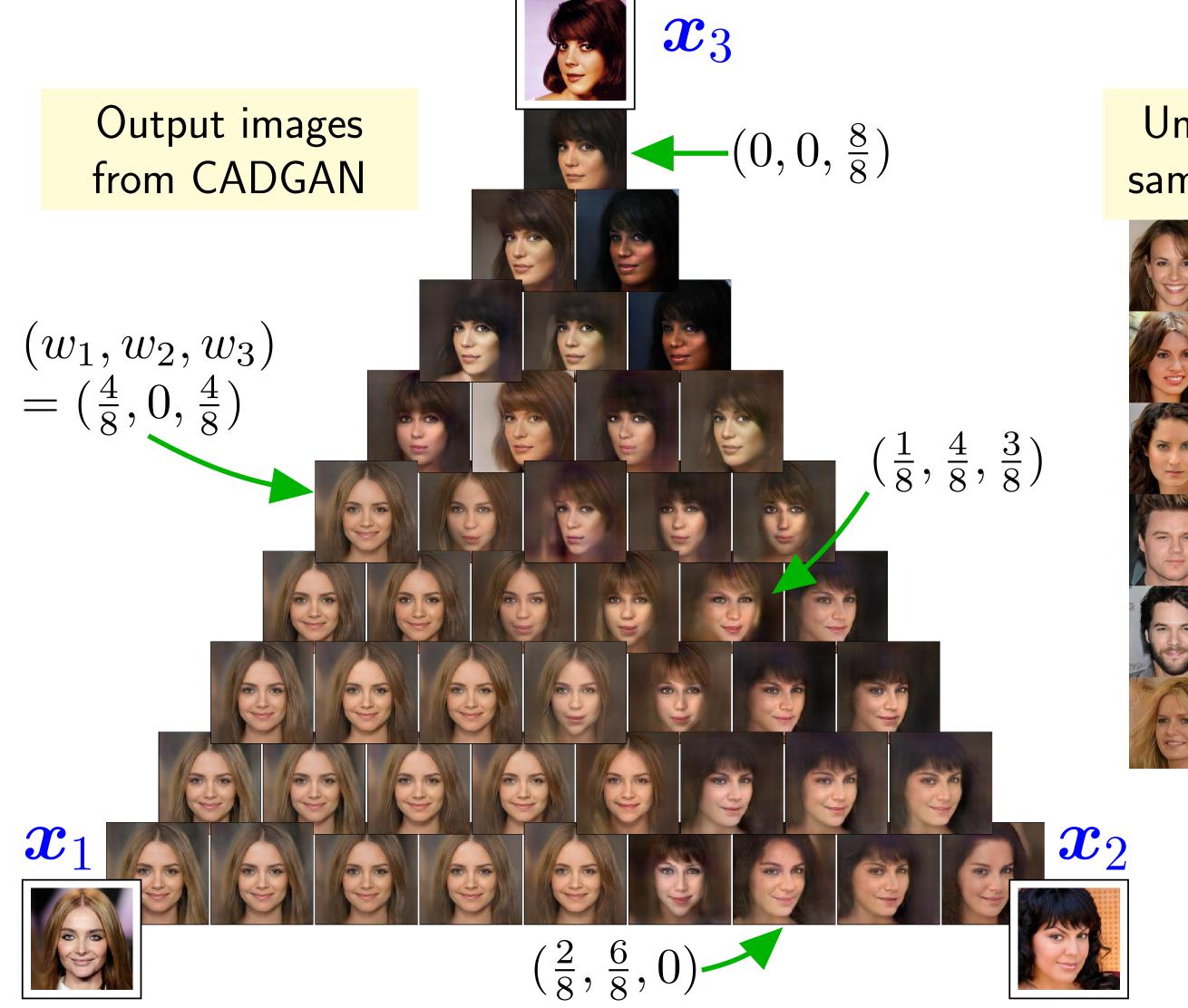
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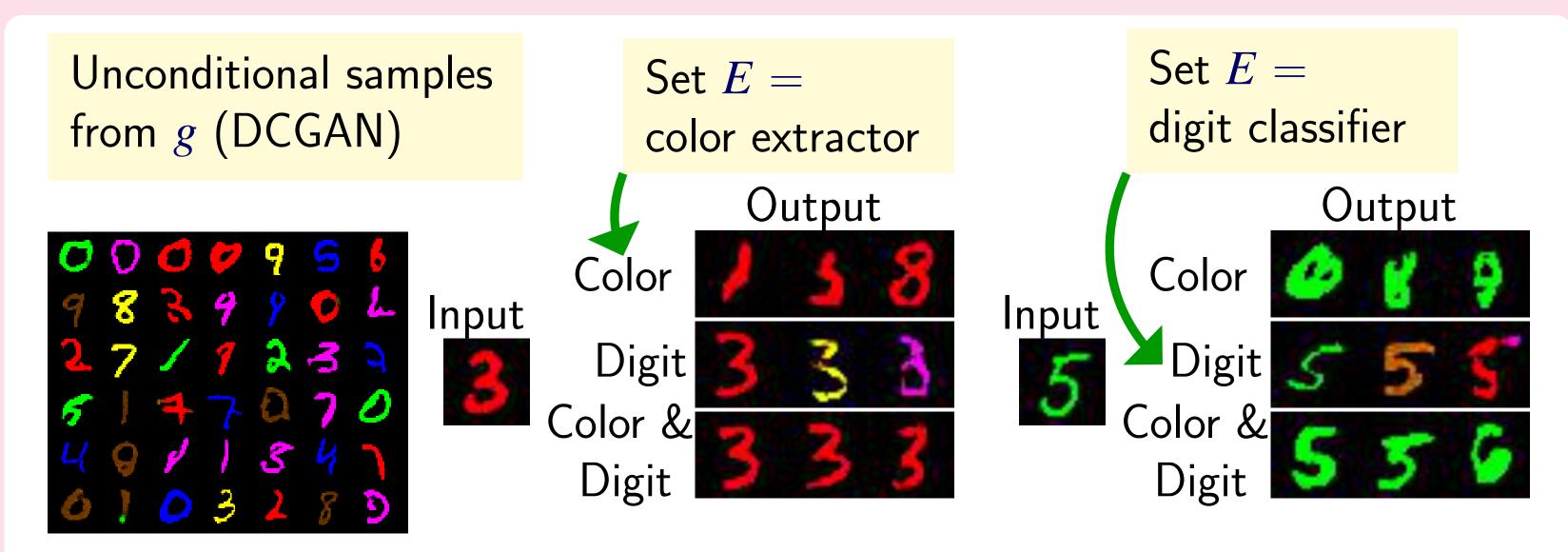


#### **Experiment:** CelebA-HQ

• g = GAN from Mescheder et al., 2018 trained on CelebA-HQ.



### **Experiment: Flexible Choice of Similarity Criterion**



Aspects of the input image(s) that will be captured can be controlled by changing the extractor E.

• For each  $(w_1, w_2, w_3)$ , generate n = 1 image from m = 3 input images.

Unconditional samples from g